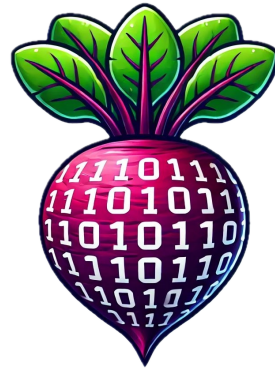




21 Million Bitcoin?

by BitRoot



1

21 Million Supply Cap?

Bitcoin Supply Formula

Bitcoin Source Code Analysis

2

Why can the Supply Cap **not** be changed?
(People have tried before!)

Basics Bitcoin Network

Who has control over Bitcoin within the Network?


Bitcoin Supply Formula

Each Term represents the **Bitcoin Block Reward** that goes to Bitcoin Miners within one Period (“Epoch”).

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

Bitcoin Supply Formula

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The current Epoch

Bitcoin Supply Formula

Each Term represents the **Bitcoin Block Reward** that goes to Bitcoin Miners within one Period (“Epoch”).

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i} \right)$$

The maximal (initial) Block Reward.

The current Epoch

Bitcoin Supply Formula

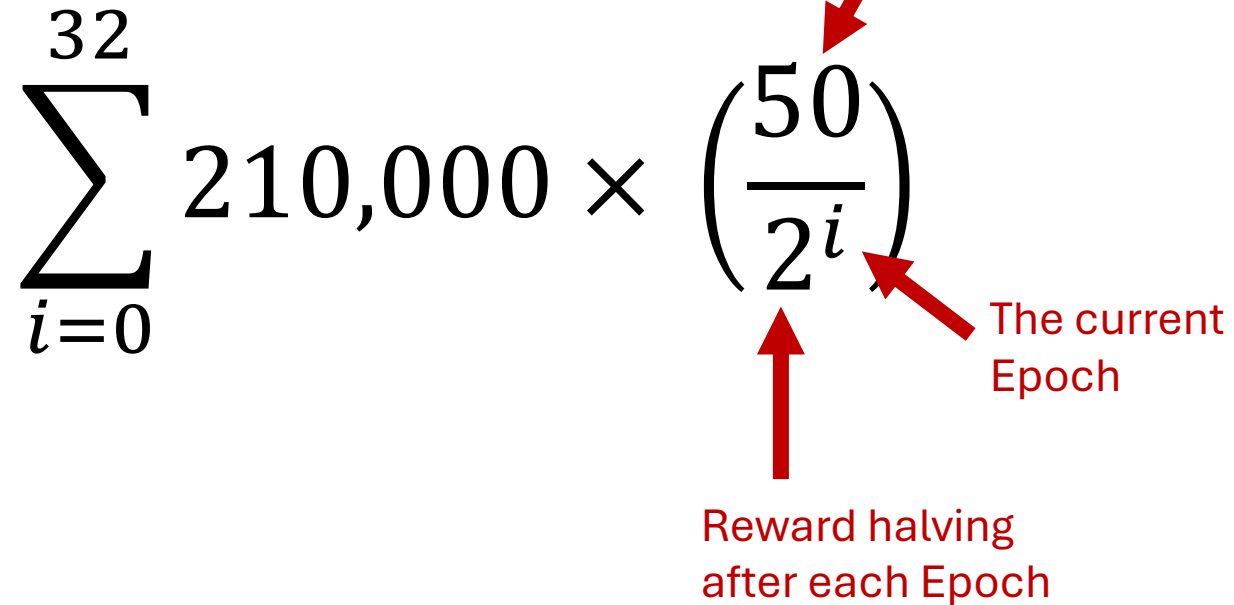
Each Term represents the **Bitcoin Block Reward** that goes to Bitcoin Miners within one Period (“Epoch”).

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i} \right)$$

The maximal (initial) Block Reward.

The current Epoch

Reward halving after each Epoch

The diagram shows the Bitcoin supply formula: a summation from i=0 to 32 of 210,000 multiplied by (50 divided by 2 to the power of i). Three red arrows point to parts of the formula: one to the 50 in the numerator, one to the 2^i in the denominator, and one to the exponent i. The arrow to 50 is labeled 'The maximal (initial) Block Reward.' The arrow to 2^i is labeled 'The current Epoch'. The arrow to i is labeled 'Reward halving after each Epoch'.

Bitcoin Supply Formula

Each Term represents the **Bitcoin Block Reward** that goes to Bitcoin Miners within one Period (“Epoch”).

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i} \right)$$

The number of Blocks mined in each Epoch (on avg. one in 10 min)

The maximal (initial) Block Reward.

The current Epoch

Reward halving after each Epoch

Bitcoin Supply Formula

Each Term represents the **Bitcoin Block Reward** that goes to Bitcoin Miners within one Period (“Epoch”).

After 33 Epochs
the Reward will have
reached 0.

$$\sum_{i=0}^{32}$$

The number of Blocks
mined in each Epoch
(on avg. one in 10 min)

210,000

×

$$\left(\frac{50}{2^i}\right)$$

The maximal (initial)
Block Reward.

The current
Epoch

Reward halving
after each Epoch

Bitcoin Supply Formula

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right) = 210,000 \times \left(\frac{50}{2^0}\right) + 210,000 \times \left(\frac{50}{2^1}\right) + \dots + 210,000 \times \left(\frac{50}{2^{32}}\right)$$

$$= 10,500,000 + 5,250,000 + \dots + 0.00000001$$

$$= 21,000,000$$

Bitcoin Supply Formula

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right) = 210,000 \times \left(\frac{50}{2^0}\right) + 210,000 \times \left(\frac{50}{2^1}\right) + \dots + 210,000 \times \left(\frac{50}{2^{32}}\right)$$

$$= 10,500,000 + 5,250,000 + \dots + 0.000000001$$

$$= 21,000,000$$

In Practice: 20,999,999.9769 Bitcoin

System discards fractional results from the halving process.

Bitcoin Supply Formula

Variables required to define the Bitcoin Supply:

1. Number of Epochs: **33**
2. Blocks mined during each Epoch: **210,000**
3. The initial Block Reward was **50 Bitcoin**.
4. Bitcoin Supply **halved** at the end of each Epoch.

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

➡ Max Bitcoin Supply: Almost 21,000,000

Source Code Analysis

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

bitcoin / src / validation.cpp

↑ Top

Code

Blame

6048 lines (5365 loc) · 286 KB

Raw



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1675      CAmount nSubsidy = 50 * COIN;
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1677      nSubsidy >>= halvings;
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Source Code Analysis

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The current block height

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Contains rules for block and transaction validation. E.g. Blocks per Epoch (210,000)

Source Code Analysis

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$$\text{halvings} = \frac{\text{Current Block Height}}{210,000}$$

In which halving cycle (epoch) are we currently?

Source Code Analysis

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

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COIN = 100,000,000
BTC to SATS calculation

Source Code Analysis

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If 'halving' (epoch) is larger than 64, no reward will be returned!

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```

Bitshift Operator

The same effect as:

$$nSubsidy = \frac{nSubsidy}{2}$$

approximately every 4 years.

Source Code Analysis

Decimal to Binary Representation

	32	16	8	4	2	1
Decimal: 1	0	0	0	0	0	1
Decimal: 2	0	0	0	0	1	0
Decimal: 3	0	0	0	0	1	1
Decimal: 35	1	0	0	0	1	1

Source Code Analysis

Right Bitshift Operator ...
moves all bits one entry to the right

Source Code Analysis

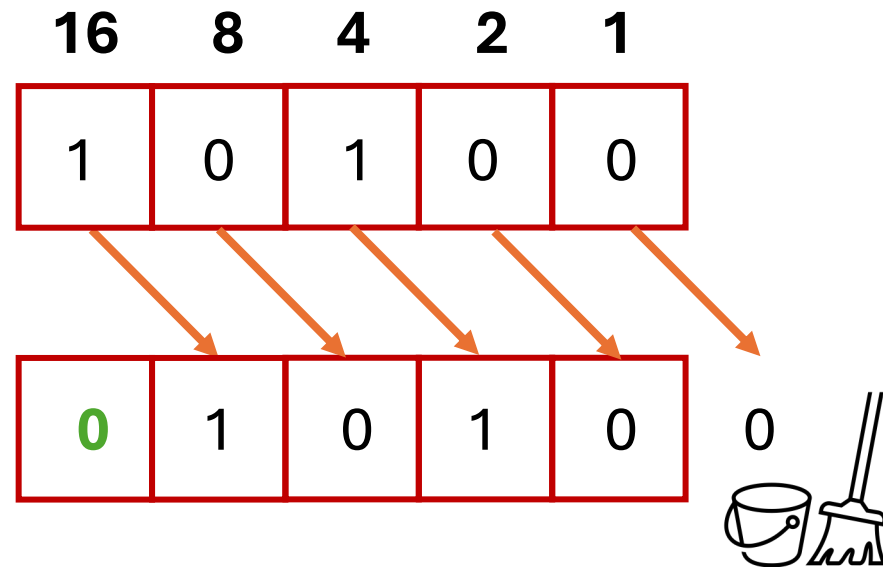
Right Bitshift Operator ...
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16	8	4	2	1
1	0	1	0	0

Decimal: 20

Source Code Analysis

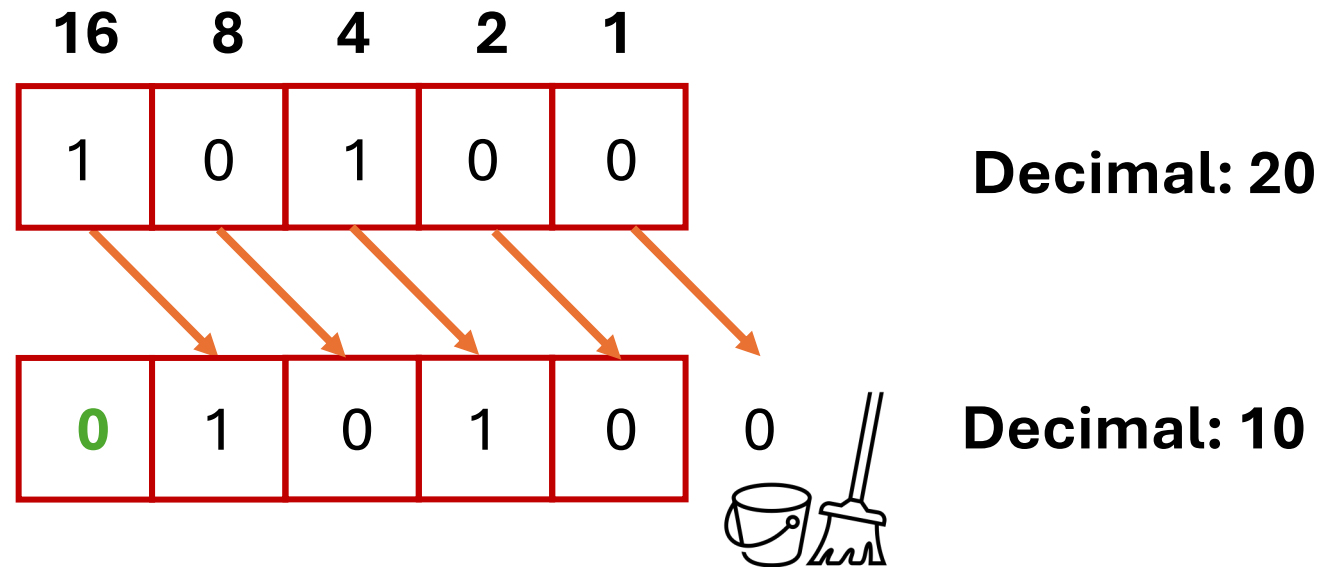
Right Bitshift Operator ...
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Decimal: 20

Source Code Analysis

Right Bitshift Operator ...
moves all bits one entry to the right



Source Code Analysis

Epoch nSubsidy

64 Bit Integer in Binary Representation

0 10010101000000101111100100000000

nSubsidy



Decimal

5,000,000,000




**First Satoshi
(5 Billion)**

Source Code Analysis

Epoch	nSubsidy	nSubsidy	
	64 Bit Integer in Binary Representation	Decimal	
0	10010101000000101111100100000000	5,000,000,000	 First Satoshi (5 Billion)
1	0 10010101000000101111100100000000 	2,500,000,000	

Source Code Analysis

Epoch	nSubsidy	nSubsidy	
	64 Bit Integer in Binary Representation	Decimal	
0	10010101000000101111100100000000	5,000,000,000	 First Satoshi (5 Billion)
1	0 10010101000000101111100100000000	2,500,000,000	
2	00 10010101000000101111100100000000	1,250,000,000	

Source Code Analysis

Epoch	nSubsidy	nSubsidy
	64 Bit Integer in Binary Representation	Decimal
0	10010101000000101111100100000000	5,000,000,000
1	01001010100000010111110010000000	2,500,000,000
2	00100101010000001011111001000000	1,250,000,000
3	00010010101000000101111100100000	625,000,000



First Satoshi
(5 Billion)

Source Code Analysis

Epoch	nSubsidy	nSubsidy
	64 Bit Integer in Binary Representation	Decimal
0	10010101000000101111100100000000	5,000,000,000
1	01001010100000010111110010000000	2,500,000,000
2	00100101010000001011111001000000	1,250,000,000
3	00010010101000000101111100100000	625,000,000
4	00001001010100000010111110010000	312,500,000



**First Satoshi
(5 Billion)**

Source Code Analysis


[illegible]


Source Code Analysis

[illegible]

Source Code Analysis

Epoch	nSubsidy	nSubsidy
	64 Bit Integer in Binary Representation	Decimal
0	100101010000001011111001000000000	5,000,000,000
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2	001001010100000010111110010000000	1,250,000,000
3	000100101010000001011111001000000	625,000,000
4	000010010101000000101111100100000	312,500,000
...		
...		
32	0000000000000000000000000000000001	1
33	0000000000000000000000000000000000	0
...		
63	0000000000000000000000000000000000	0

**First Satoshi
(5 Billion)**

**Last Satoshi**

Source Code Analysis

Epoch	nSubsidy 64 Bit Integer in Binary Representation	nSubsidy Decimal
0	1001010100000010111111001000000000	5,000,000,000
1	0100101010000001011111001000000000	2,500,000,000
2	0010010101000000101111100100000000	1,250,000,000
3	0001001010100000010111110010000000	625,000,000
4	0000100101010000001011111001000000	312,500,000
...		
...		
32	0000000000000000000000000000000001	1
33	0000000000000000000000000000000000	0
...		
63	0000000000000000000000000000000000	0
64		UNDEFINED

Source Code Analysis

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

bitcoin / src / validation.cpp

↑ Top

Code

Blame

6048 lines (5365 loc) · 286 KB

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1675      CAmount nSubsidy = 50 * COIN;
1676      // Subsidy is cut in half every 210,000 blocks (~4 years)
1677      nSubsidy >>= halvings;
1678      return nSubsidy;
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```

After 64 Bitshift Operations, the Code will return 'undefined' and ERROR!

Source Code Analysis

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```

Why don't check:

if (halvings >= 33)
 return 0;

After we reached epoch number 33,
nSubsidy will be 0 anyway!

Mathematical Adjustment - Bitcoin Supply from 21 to 210 Million

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

Mathematical Adjustment - Bitcoin Supply from 21 to 210 Million

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

Larger initial Bitcoin Reward

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{500}{2^i}\right)$$

Mathematical Adjustment - Bitcoin Supply from 21 to 210 Million

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{50}{2^i}\right)$$

Larger initial Bitcoin Reward

$$\sum_{i=0}^{32} 210,000 \times \left(\frac{500}{2^i}\right)$$

Increased Speed of Block creation

$$\sum_{i=0}^{32} 2,100,000 \times \left(\frac{50}{2^i}\right)$$

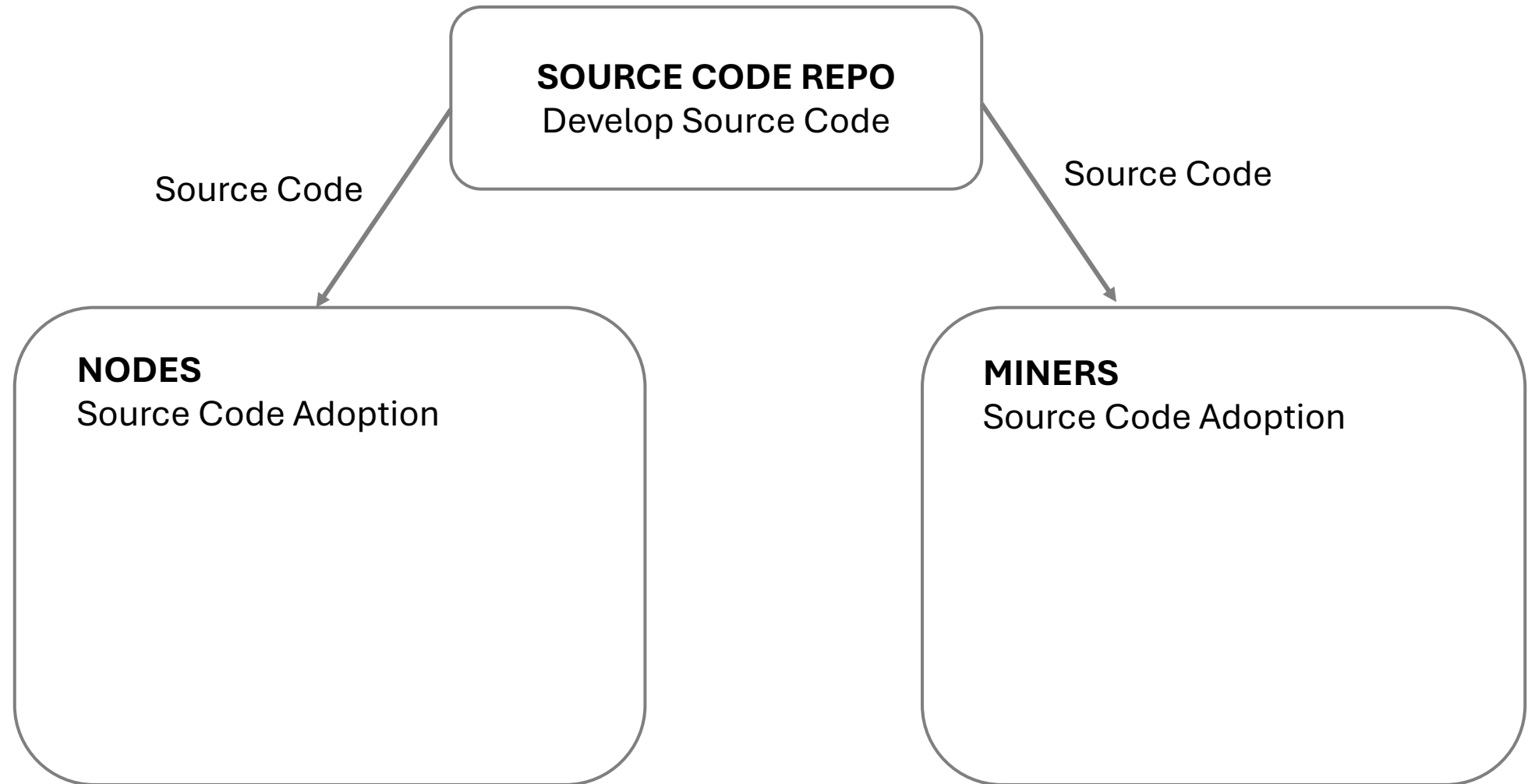


Why can the Supply Cap
not be changed?
(People have tried!)

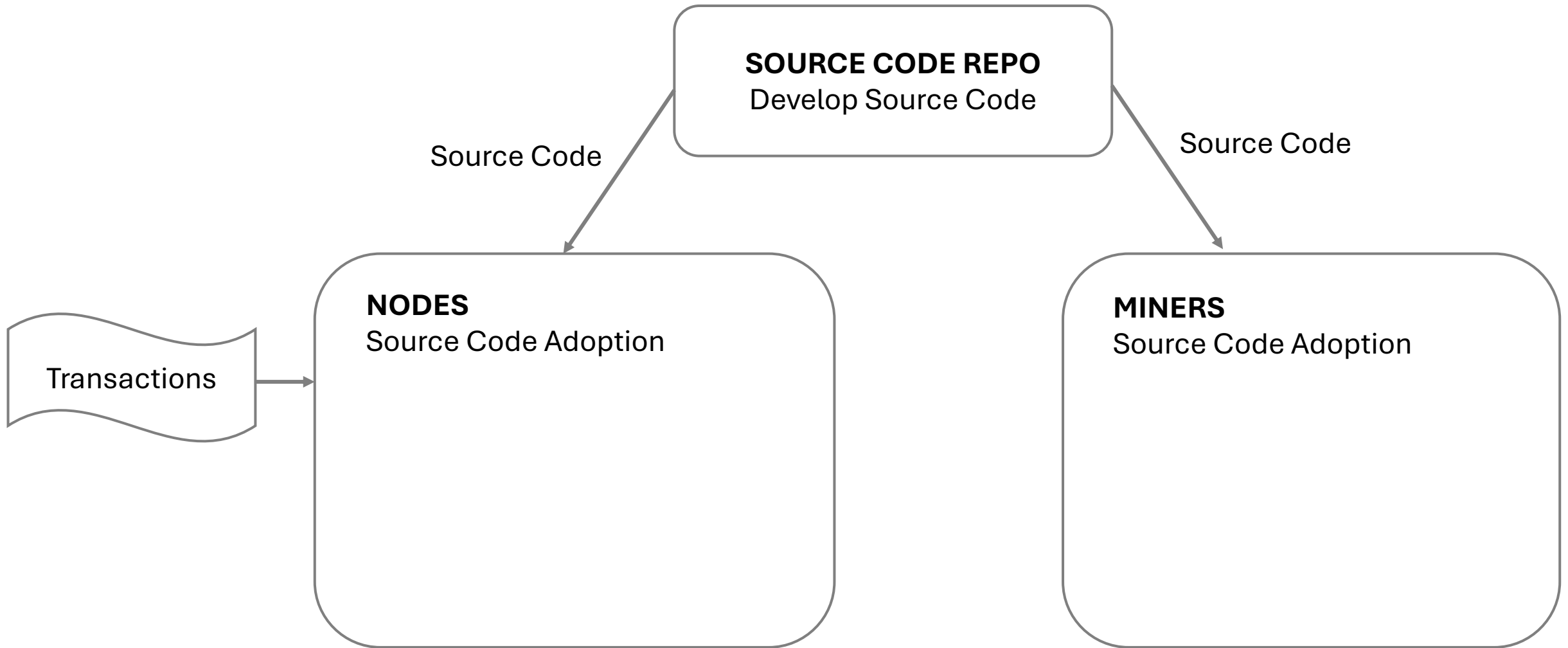
Bitcoin Network

SOURCE CODE REPO
Develop Source Code

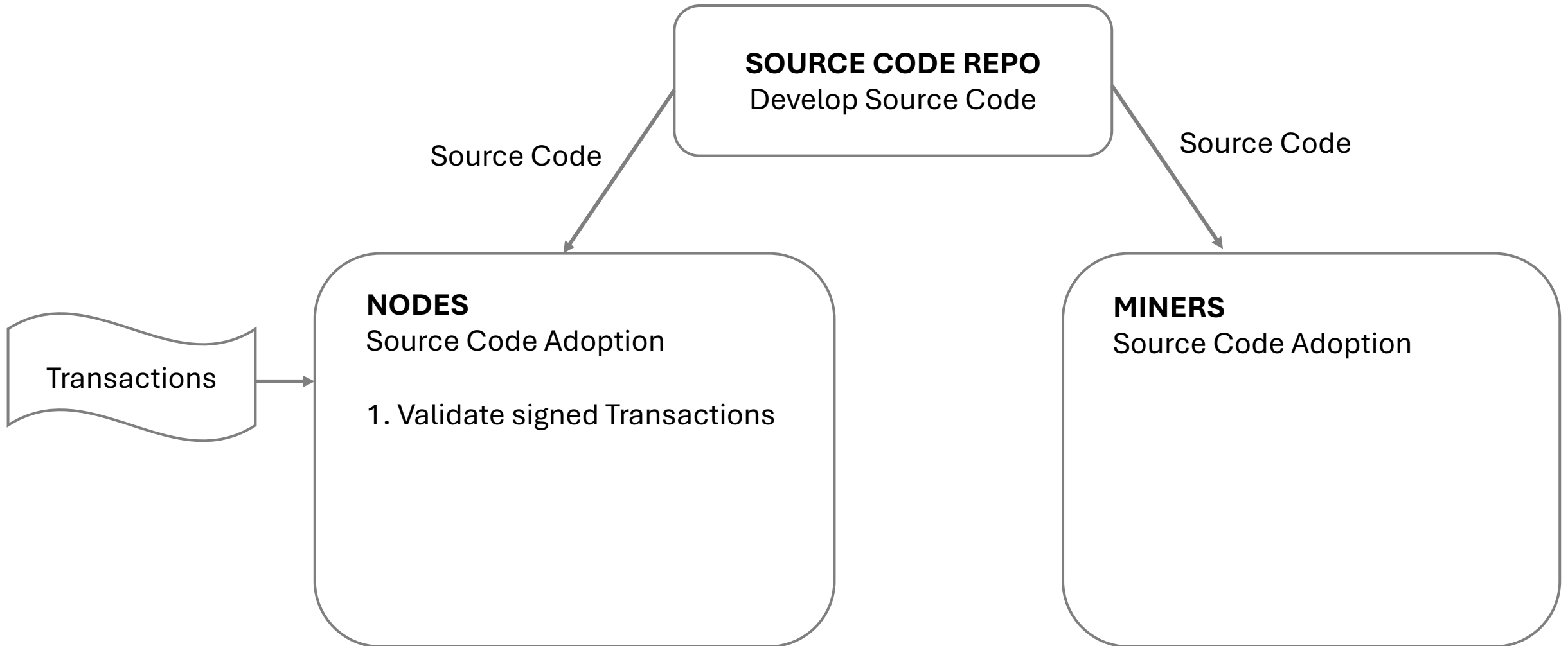
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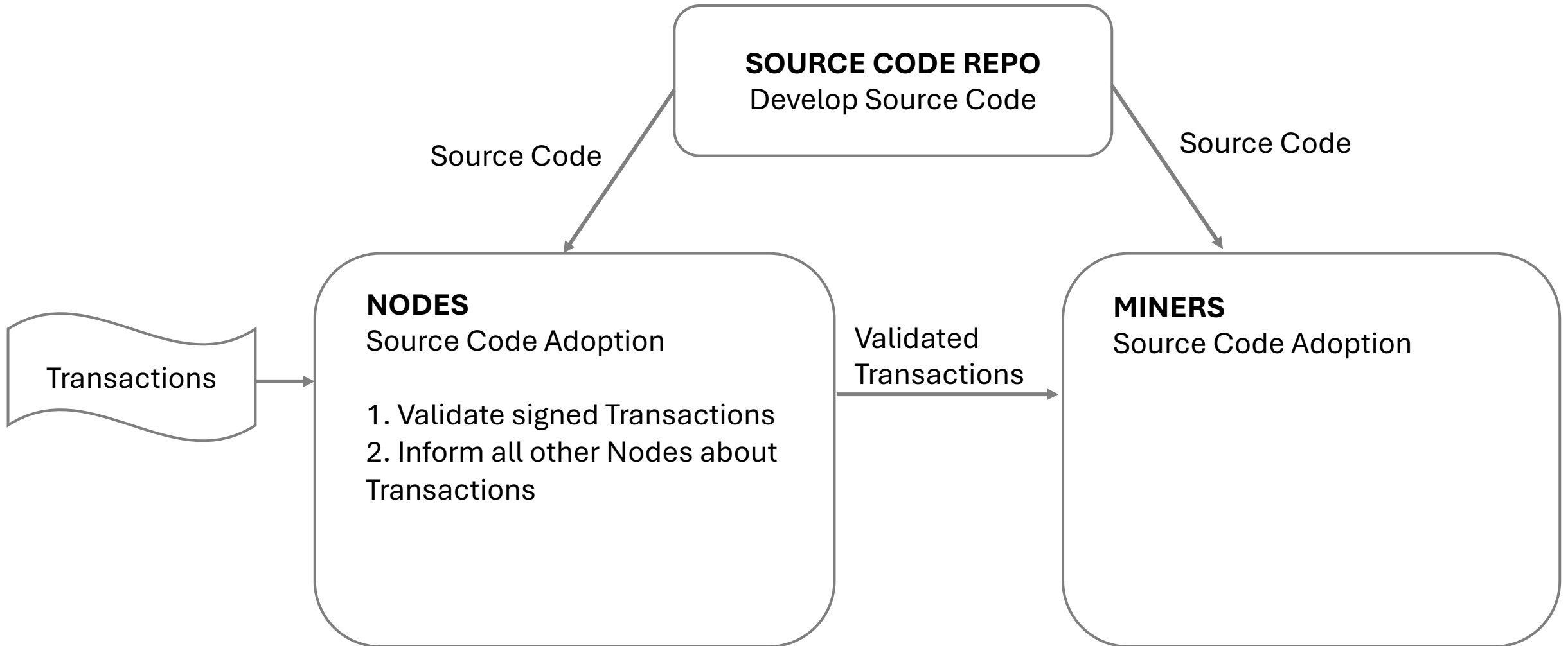
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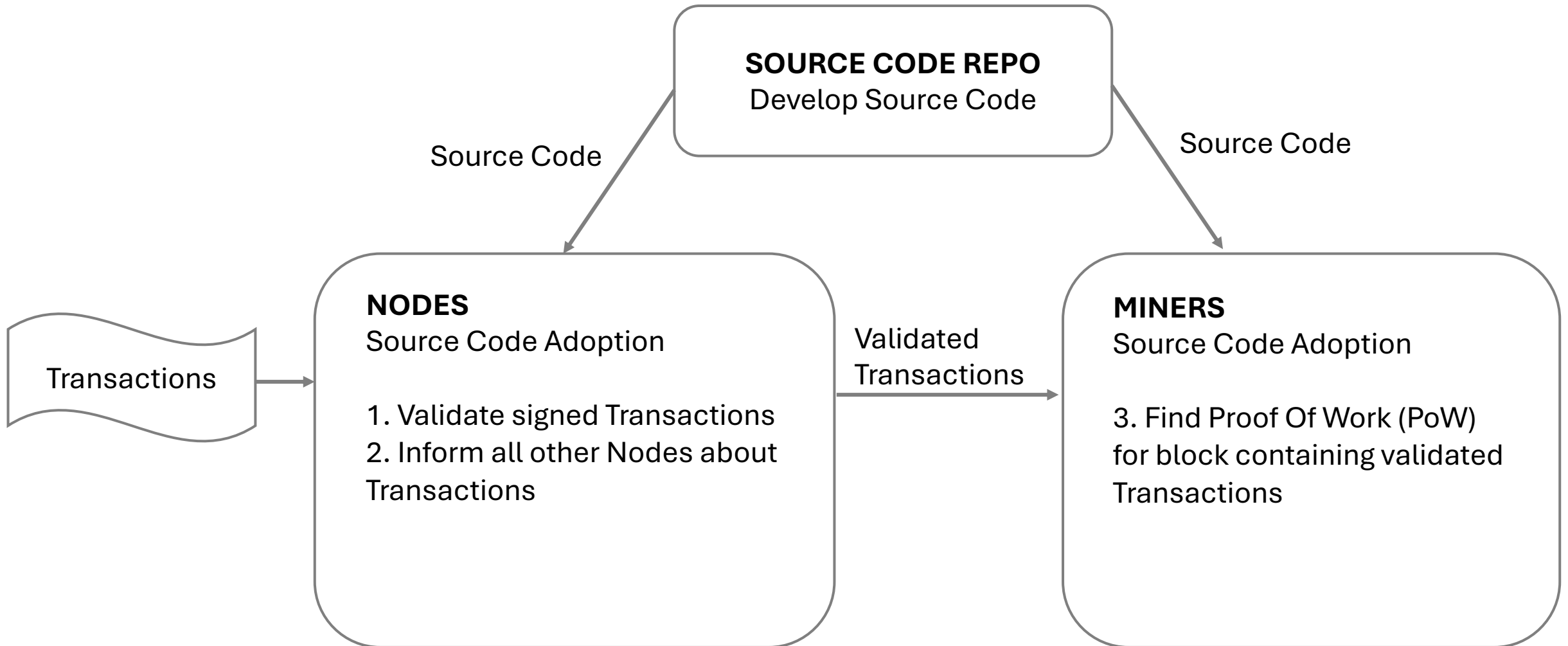
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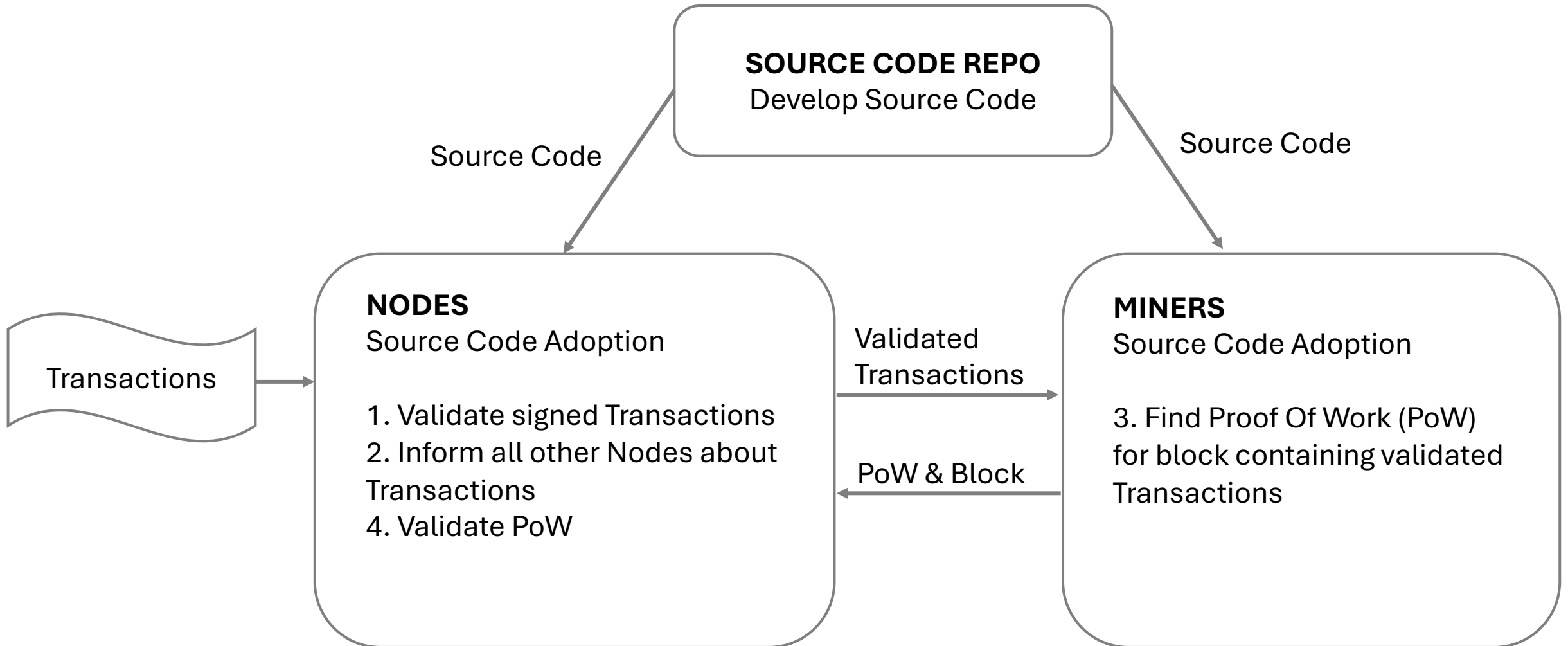
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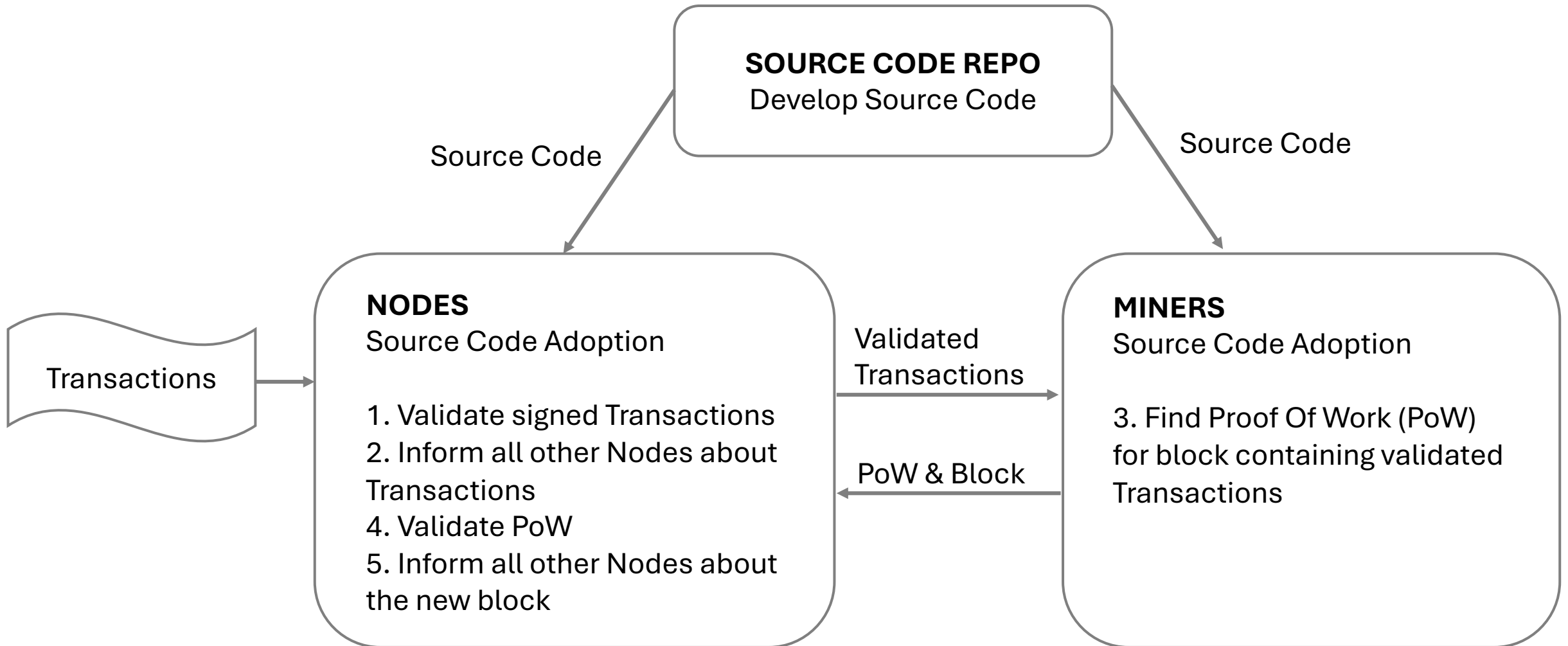
Bitcoin Network



Bitcoin Network



Bitcoin Network



Source Code Developers control Bitcoin?



SOURCE CODE REPO

Source Code Developers control Bitcoin?

Anyone can contribute to the Source Code!

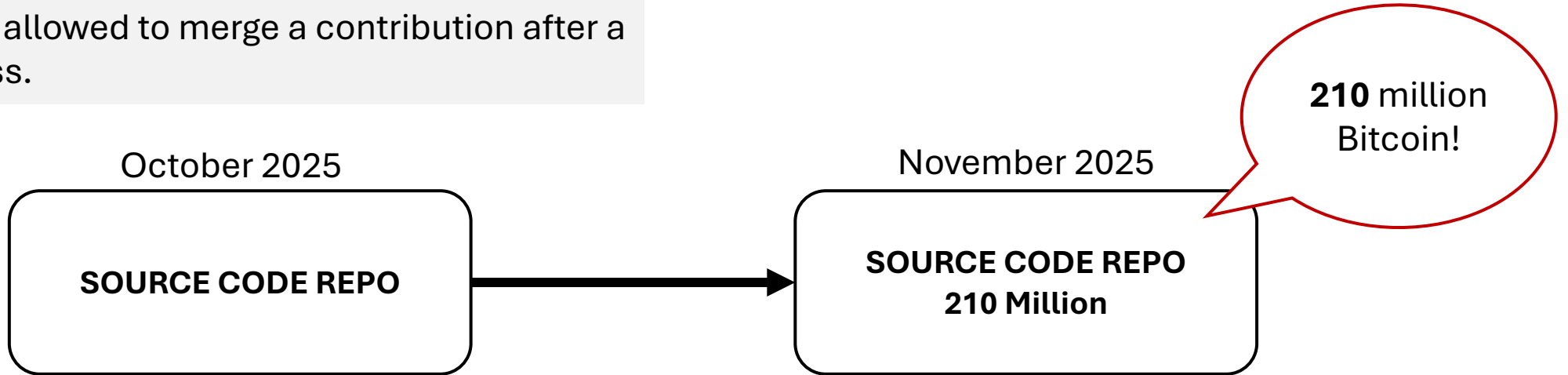
Maintainers are allowed to merge a contribution after a reviewing process.

SOURCE CODE REPO

Source Code Developers control Bitcoin?

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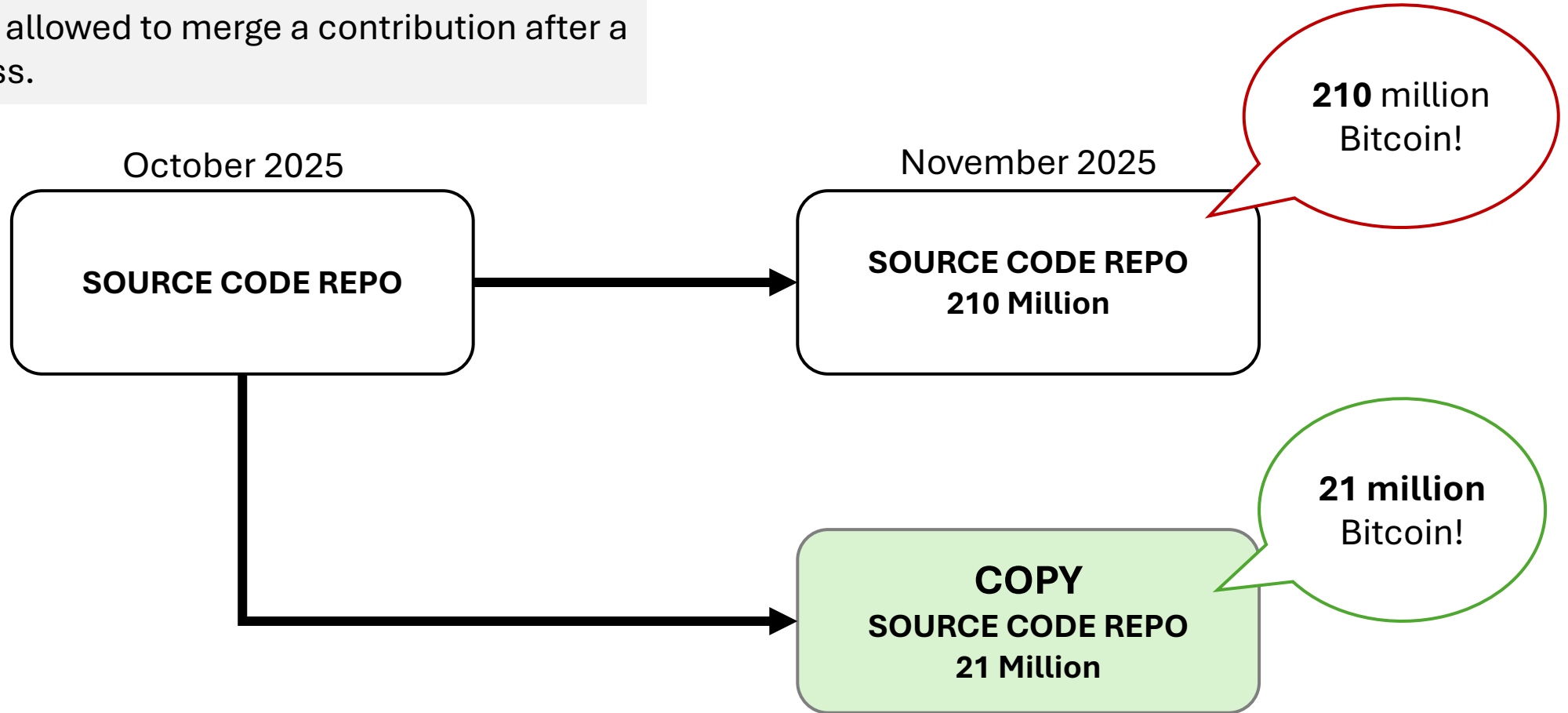
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Source Code Developers control Bitcoin?

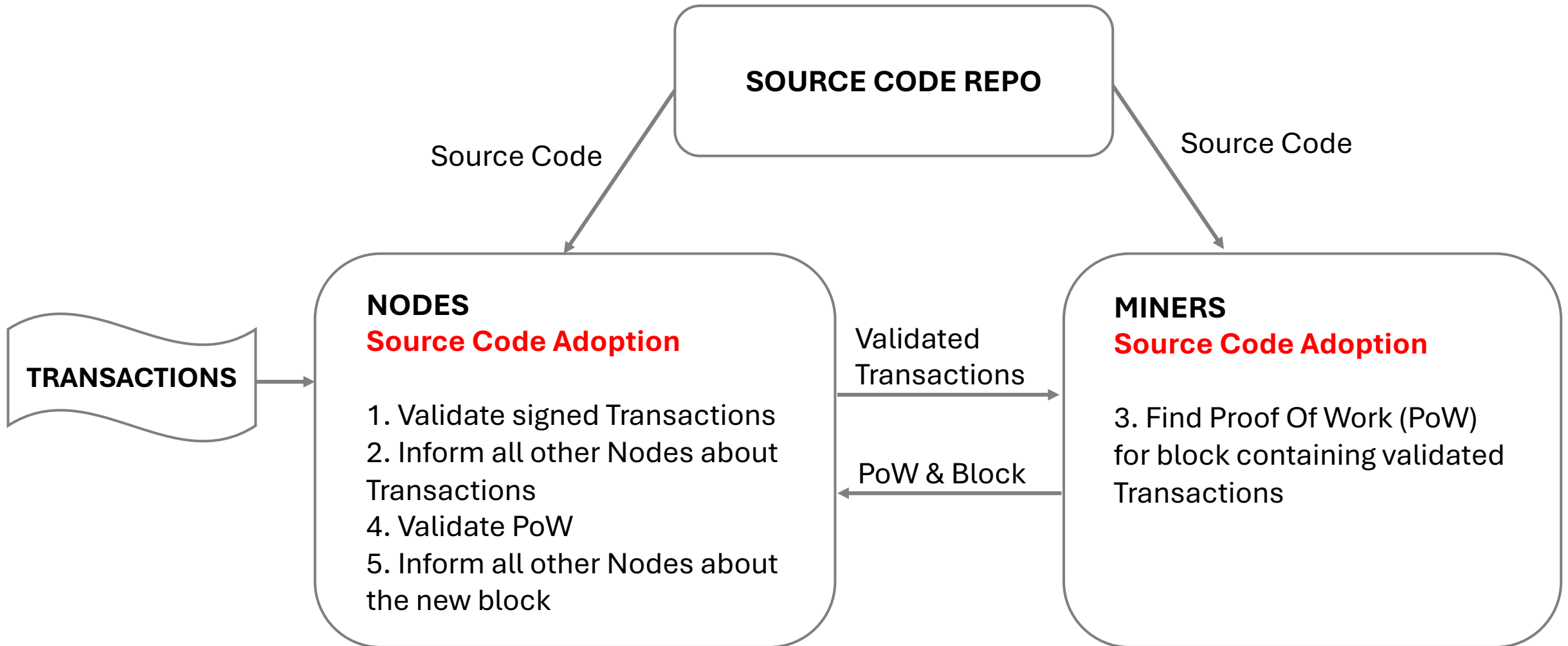
Yes!

Developers can introduce significant changes!

And No!

- *Anyone* can introduce source code changes!
- *Anyone* can copy a repository!
- No one can force owners of miners and nodes to run a specific software.

Owner of Miners and Nodes control Bitcoin?



Owner of Miners and Nodes control Bitcoin?

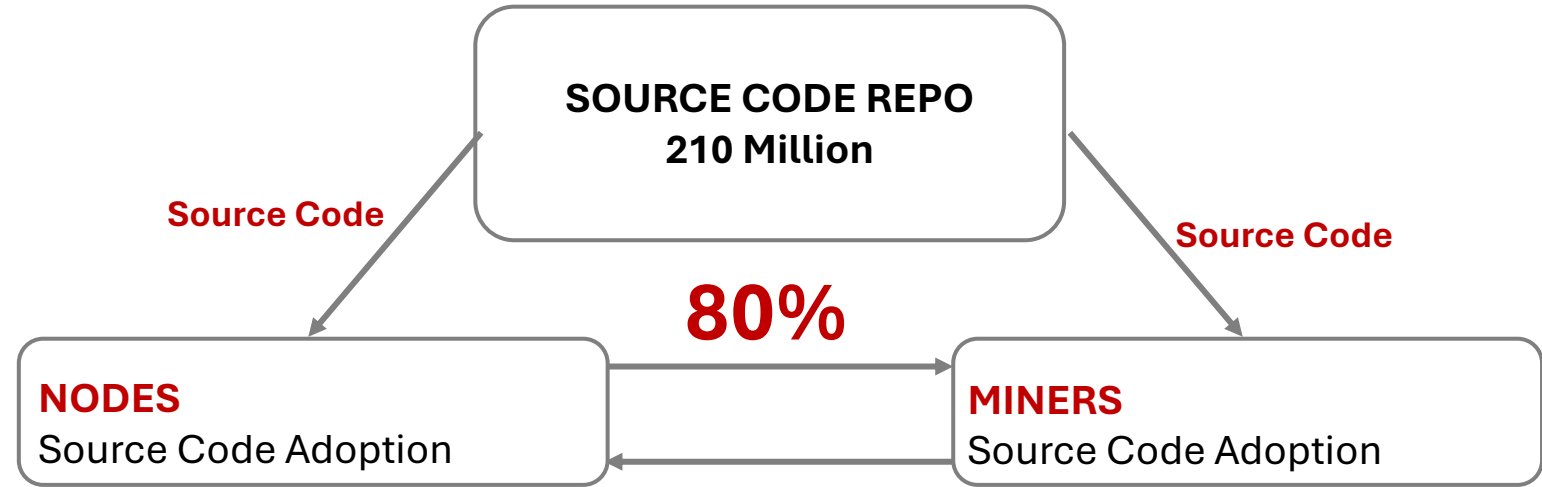
Yes!

Miners and nodes can choose which repositories to upgrade from.

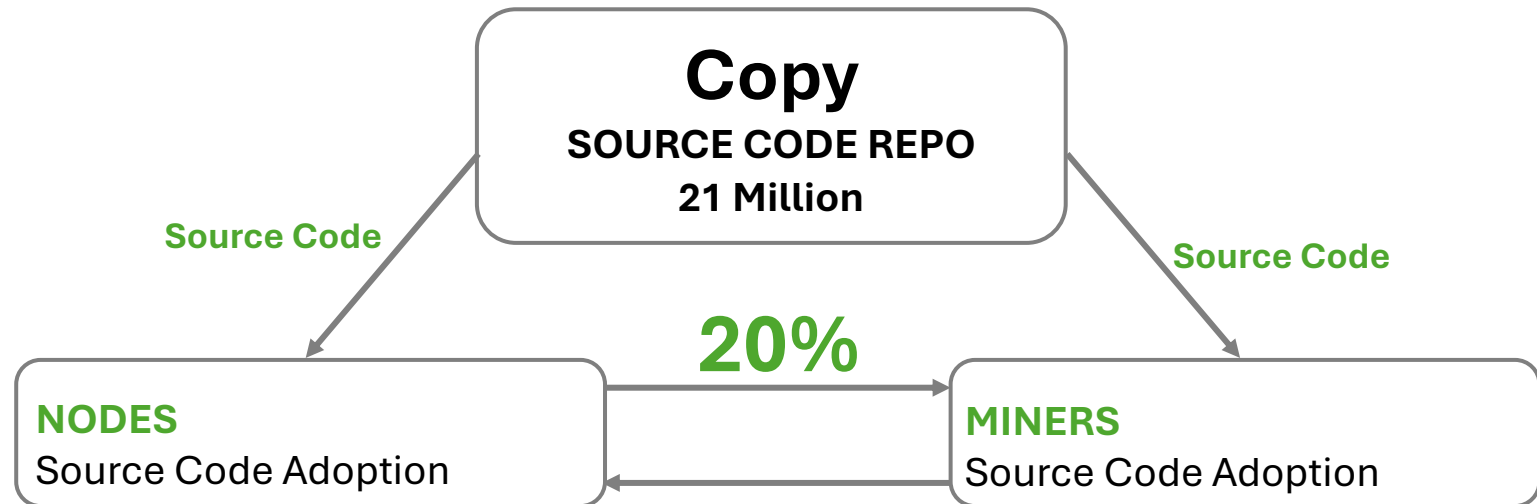
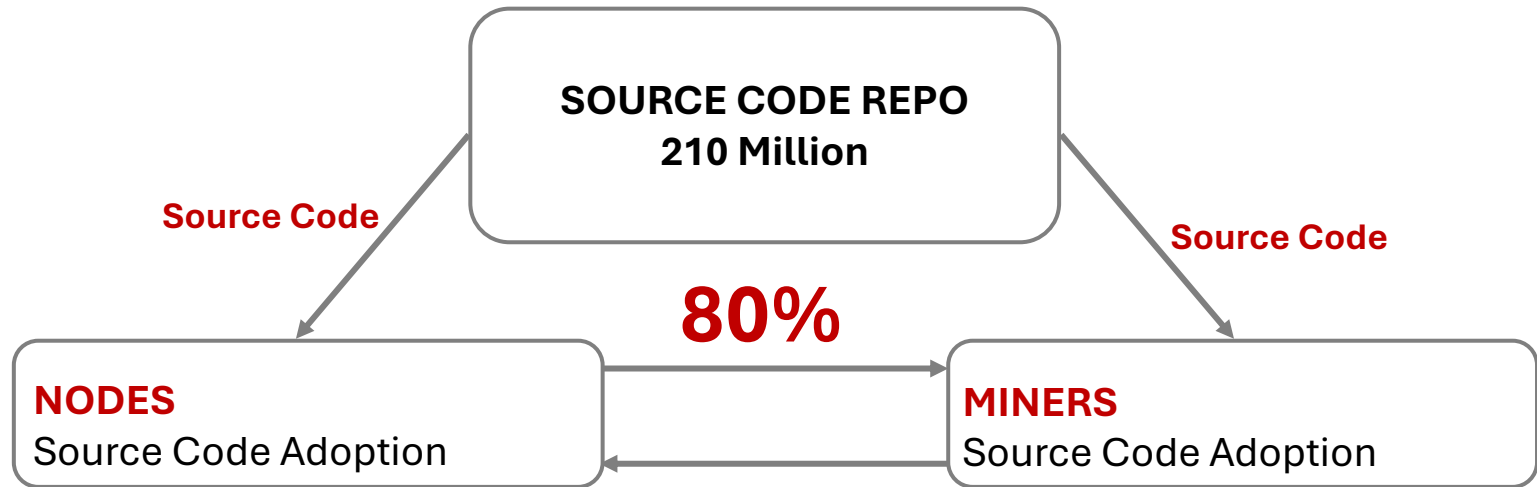
And No!

- Anyone can run a node or miner using their *preferred* source code repository.
- No one can force Bitcoin hodlers to execute transactions through specific nodes and miners.

What happens if...

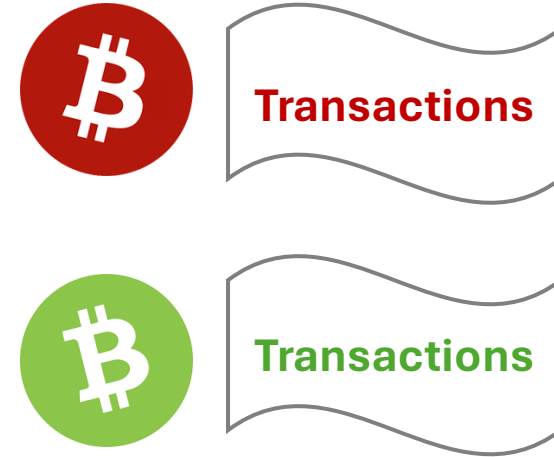


What happens if...



Hodlers control Bitcoin?

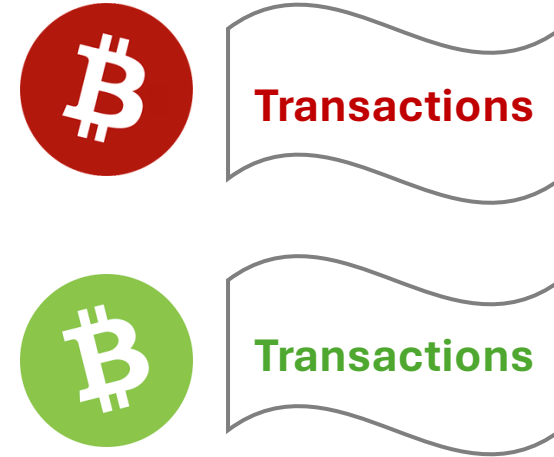
Owners **receive an equivalent amount of the new Bitcoin version** on the new, separate blockchain.



Hodlers control Bitcoin?

Owners **receive an equivalent amount of the new Bitcoin version** on the new, separate blockchain.

All Hodlers can now **trade both** Bitcoin Versions.



Hodlers control Bitcoin?

Yes!

You can decide which Bitcoin is more valuable through your buying and selling power.

And No!

You might lose out by acting against the majority, as your individual decision is not enough to control adoption.

Previous Attempt to increase the Bitcoin Supply

24th November 2017

Bitcoin Diamond was a hard fork of the Bitcoin blockchain to increase the Bitcoin supply to **210 Million**.

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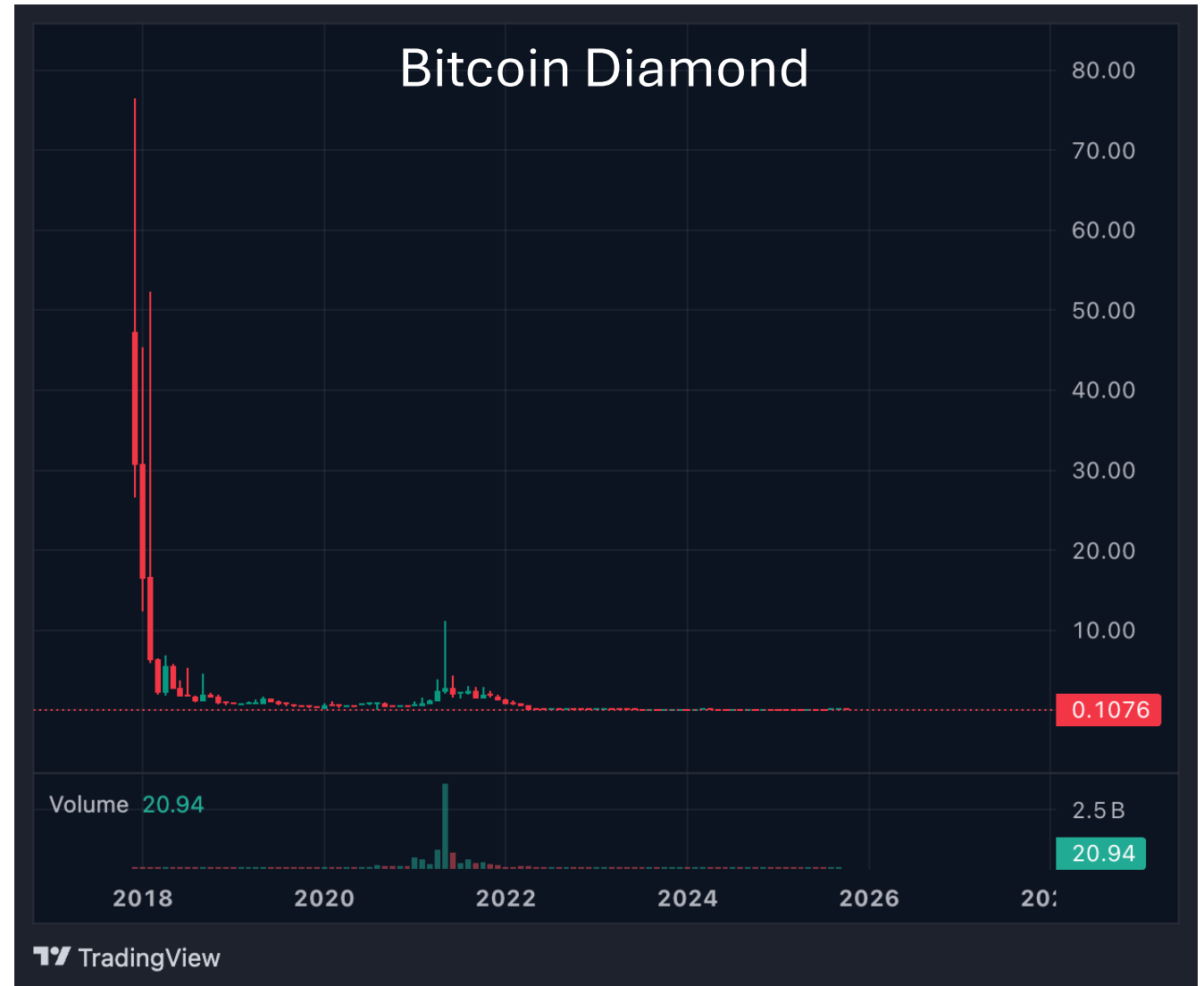
November 2017

Bitcoin: \$8

November 2025

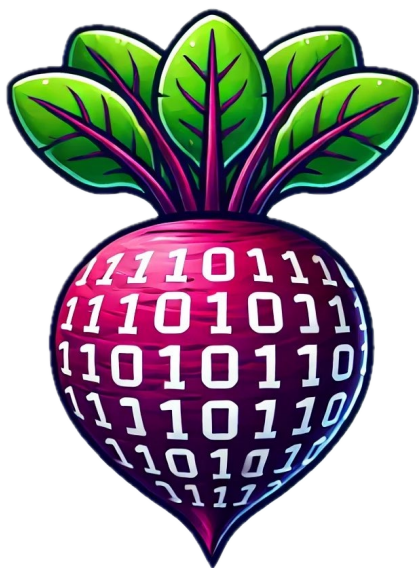
Bitcoin: \$ 115,000

Bitcoin Diamond: \$0.10





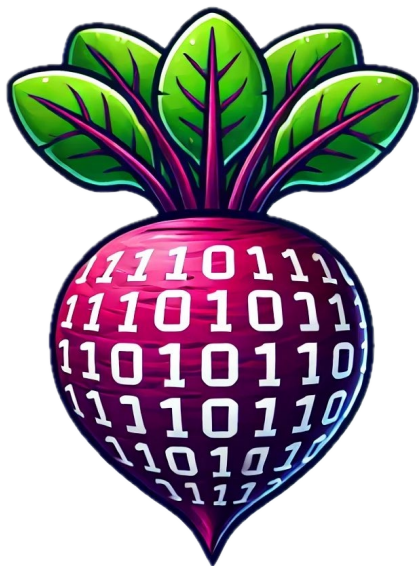
**Yes, everyone and
no, no one** has
control over Bitcoin
and its supply cap.



bitroot.me



bitroot@zaps.lol



bitroot.me



bitroot@zaps.lol



cyphermunkhouse.com